

## Solution “Machine Structure 1” “Final Exam” 1/3 23/24

EXO1 (6pts)

1)

11a) First method with successive division

$$\begin{array}{r}
 1457 \quad | \quad 16 \\
 1 \quad | \quad 91 \quad | \quad 16 \\
 11 \quad | \quad 5 \quad | \quad 16 \\
 \hline
 5 \quad | \quad 0
 \end{array}
 \qquad
 \begin{array}{r}
 0.11 \\
 \times 16 \\
 \hline
 (1).76 \\
 \times 16 \\
 \hline
 (12).16
 \end{array}$$

$(5 \ 11 \ 1 \ . \ 1 \ 12)_10$  corresponds in hexadecimal to 5B1.1C  
 $(1457)_{10} = (5B1.1C)_{16}$  (2pts)

11b) Second method we convert to binary the integer part

2048	1024	512	256	128	64	32	16	8	4	2	1
0	1	0	1	1	0	1	1	0	0	0	1

$$(1457)_{10} = (0101 \ 1011 \ 0001)_2 = (5B1)_H$$
 (1pt)

Now we convert the fractional part by multiplying by 16 we get:

$$0.11 \times 16 = 1.76 \text{ we take } 1$$

$$0.76 \times 16 = 12.16 \text{ we take } 12 \text{ which corresponds to C in hexadecimal base}$$

$$\text{Therefore } 1457.11_{10} = (5B1.1C)_H \text{ (1pt)}$$

b) To convert from base 16 to base 4. The base 4 is includes in base 16 then We divide this number 5B1.1C by 4 it gives (11 23 01.01 03)<sub>4</sub>

$$(5B1.1C)_H = (112301.0103)_4 \text{ (2pts)}$$

2) negative sign s= 1  $(10100111.1001)_2$  we normalize  $1.0100111001 \times 2^7$  e=7

$$E=7+127=(134)_{10} \text{ in binary we get } (10000110)_2$$

Single precision: 1 10000110 010011100100000000000000 (2pts)

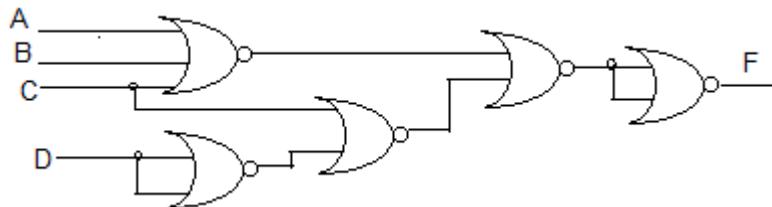
EXO2 (4pts)

$BC'D' + ABC' + AC'D + AB'D + A'BD'$  By using Consensus theorem :  $XY + X'Z + YZ = XY + X'Z$  we take the terms  $ABC'$  and  $AB'D$  to eliminate  $AC'D$  in one hand , in the other hand we take the terms  $ABC'$  and  $A'BD'$  to eliminate  $BC'D'$  in using the consensus theorem (2pts)

$$BC'D' + ABC' + AC'D + AB'D + A'BD' = ABC' + AB'D + A'BD' \quad (2\text{pts})$$

EXO3 (4pts)

$$F = \bar{A}\bar{B}\bar{C} + \bar{C}D = \overline{\overline{\bar{A}\bar{B}\bar{C}} + \bar{C}D} = \overline{\overline{\bar{A}\bar{B}\bar{C}} \cdot \overline{\bar{C}D}} = \overline{(A + B + C) \cdot (C + \bar{D})} = \overline{\overline{\overline{(A + B + C)} \cdot \overline{(C + \bar{D})}}} = \overline{\overline{\overline{(A + B + C)}} + \overline{\overline{(C + \bar{D})}}} \quad (2 \text{ pts})$$



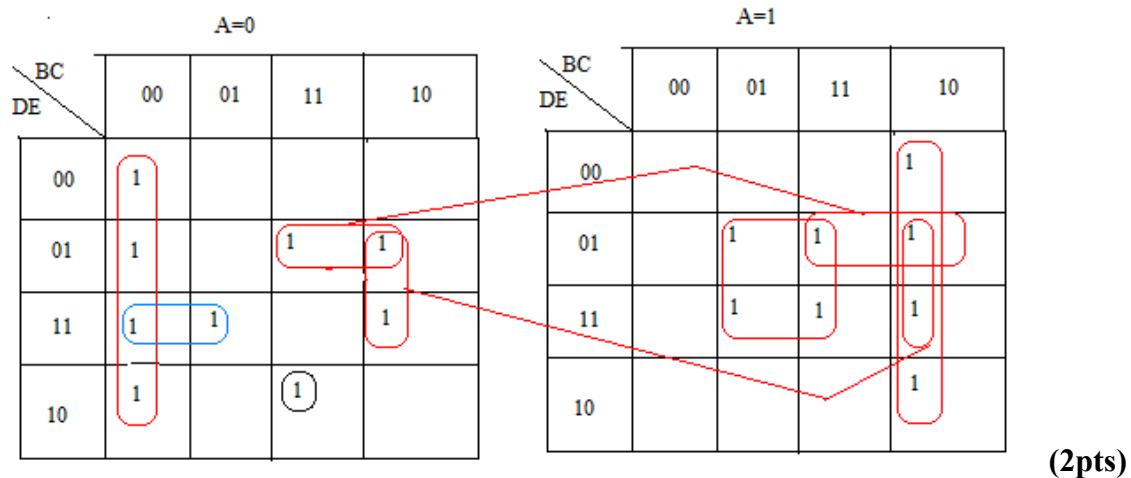
(2 pts)

EXO4 (6pts)

- (a) Prime Implicants (8) :  $A'B'C'$ ,  $BD'E$ ,  $ACE$ ,  $ABC'$ ,  $A'B'DE$ ,  $A'BCDE'$ ,  $BC'E$ ,  $A'C'E$  (1pt)
- (b) Essential PI (6) :  $A'B'C'$ ,  $BD'E$ ,  $ACE$ ,  $ABC'$ ,  $A'B'DE$ ,  $A'BCDE'$  (1pt)
- (c) Minimizing

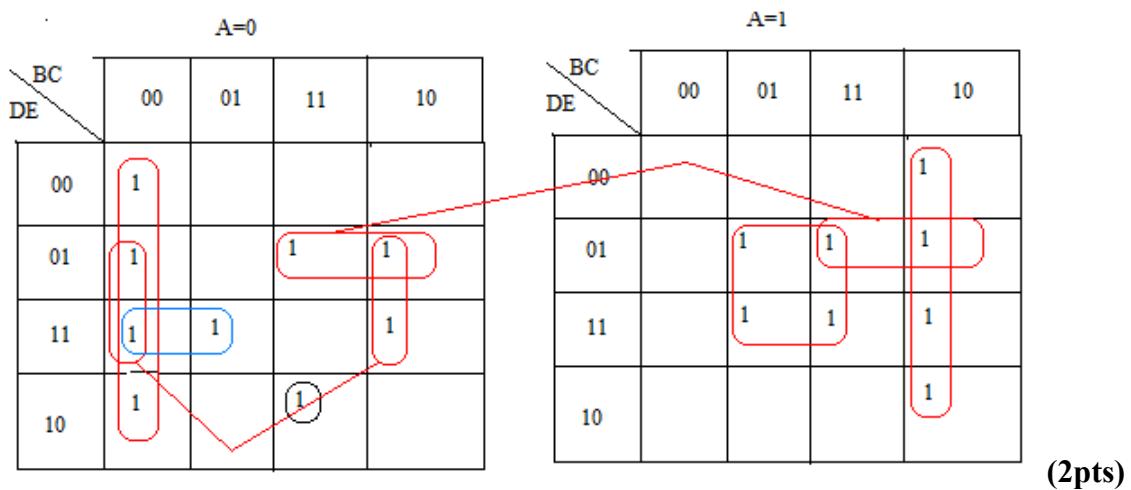
## Solution “Machine Structure 1” “Final Exam” 3/3 23/24

First solution



$$F(A, B, C, D, E) = A'B'C' + BD'E + ACE + ABC' + A'B'DE + A'BCDE' + BC'E \quad (2\text{pts})$$

Second solution



$$F(A, B, C, D, E) = A'B'C' + BD'E + ACE + ABC' + A'B'DE + A'BCDE' + A'C'E \quad (2\text{pts})$$